Week 4: Compound Interest



- MA120: Personal Finance
- Instructor: Rebecca Lombardo
- Week of April 20, 2015

Review of Simple Interest: I = p r t

- 1.) Luther puts \$300 in a savings account paying 0.53% interest. How long will it take to earn \$50 in interest?
- 2.) Tanesha is looking to put \$150 into a savings account. What interest rate does she need a savings account to have in order to have a total of \$200 in the bank account 1 year from now?

Review of Simple Interest: I = p r t

- 1.) Luther puts \$300 in a savings account paying 0.53% interest. How long will it take to earn \$50 in interest?
- I = p r t
- t = I / pr
- $t = $50 / $300 \times 0.53\%$
- t = 50 / (300 x 0.0053)
- <u>t = 31.34 yrs</u>

2.) Tanesha is looking to put \$150 into a savings account. What interest rate does she need a savings account to have in order to have a total of \$200 in the bank account 1 year from now?

Review of Simple Interest: I = p r t

 Luther puts \$300 in a savings account paying 0.53% interest. How long will it take to earn \$50 in interest? 	2.) Tanesha is looking to put \$150 into a savings account. What interest rate does she need a savings account to have in order to have a total of \$200 in the bank account 1 year from now?
l = p r t	
t = I / pr	r = I / p t I = $200 - 150 = 50$
t = \$50 / \$300 x 0.53%	r = \$50 / (\$150 x 1)
t = 50 / (300 x 0.0053)	r = 0.333 = <u>33.3%</u>
<u>t = 31.34 yrs</u>	



Students will use the compound interest formula to calculate the interest earned and total money in a savings account.

Compound Interest



Compound Interest

Interest on savings account – if not withdrawn – is added to the principal after a set amount of time. This forms a <u>new</u> principal. The new principal earns interest for the next period of time, and then this new amount of interest gets added to form another new principal. At the end of each period of time, we have a new, higher principal! This process is known as <u>compound interest</u>.

Interest is compounded (added to the principal) after a set constant amount of time...usually at the end of each year, half year, or quarter year.



Annually

Semi-annually

Quarterly

Annually – once a year
 Semi-annually
 Quarterly

Annually – once a year

Semi-annually – 2x a year (every 6 mos)

Quarterly

Annually – once a year

Semi-annually – 2x a year (every 6 mos)

Quarterly – 4x a year (every 3 mos)

♦ Generally <u>compound</u> <u>interest</u> is applied to man financial products → savings accounts, loans, credit cards, life insurance etc.



In terms of our formula:

Simple Interest: I = ptr A = p + I

Compound Interest: you must do calculations for A for <u>each</u> year of the loan

Year #	Principal (p)	Interest Rate (r)	Time (t)	l = prt	Year End Amount (A = I + p)

Year #	Principal (p)	Interest Rate (r)	Time (t)	l = prt	Year End Amount (A = I + p)
1	\$600	0.04	1		
2					
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	
2					
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2					
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2	\$624				
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
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2	\$624	0.04			
3					

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2	\$624	0.04	1		
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2	\$624	0.04	1	I = 624 x 0.04 x 1 = \$24.96	
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2	\$624	0.04	1	I = 624 x 0.04 x 1 = \$24.96	\$648.96
3					

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2	\$624	0.04	1	I = 624 x 0.04 x 1 = \$24.96	\$648.96
3	\$648.9 6				

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3	\$648.9 6	0.04	1	\$25.96	

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3	\$648.9 6	0.04	1	\$25.96	<u>\$674.92</u>

How much total <u>interest</u> did you earn?

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3	\$648.9 6	0.04	1	\$25.96	<u>\$674.92</u>

- How much total <u>interest</u> did you earn?
 - A = I + p \$674.92 = I + \$600

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- How much total <u>interest</u> did you earn?
 - A = I + p \$674.92 = I + \$600 I = \$74.92 over 3 yrs

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$600	0.04	1	I = 600 x 0.04 x 1 = \$24	A= 600+ 24= \$624
2	\$624	0.04	1	I = 624 x 0.04 x 1 = \$24.96	\$648.96
3	\$648.9 6	0.04	1	\$25.96	<u>\$674.92</u>

- 2.) You earn 1¹/₂ % interest, compounded annually, on your \$2500 investment.
- a) Using the table below, calculate how much your investment will be worth after 3 years. Total I = 2614.19 2500 = 114.19

Year #	Principal (p)	Interest Rate (r)	Time (t)	l = prt	Year End Amount (A = I + p)
1	\$2500				
2					
3					

- 2.) You earn 1¹/₂ % interest, compounded annually, on your \$2500 investment.
- a) Using the table below, calculate how much your investment will be worth after 3 years. Total I = 2614.19 2500 = 114.19

Year #	Principal (p)	Interest Rate (r)	Time (t)	I = prt	Year End Amount (A = I + p)
1	\$2500	0.015	1	\$37.50	\$2537.50
2	\$2537.5 0	0.015	1	\$38.06	\$2575.56
3	\$2575.5 6	0.015	1	\$38.63	<u>\$2614.19</u>

- 3.) You earn 7.5% interest compounded <u>semi-annually</u> on your \$3000 investment.
- a) Using the grid below, create a table to calculate how much your investment will be worth after 2 years.

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Year #	Principal (p)	Interest Rate (r)	Time (t)	l = prt	Year End Amount (A = I + p)
0.5yr	\$3000	0.075	0.5	\$112.50	\$3112.50
1 yr	\$3112.50	0.075	0.5	\$	
1 5					

1.5 yr

- 3.) You earn 7.5% interest compounded <u>semi-annually</u> on your \$3000 investment.
- a) Using the grid below, create a table to calculate how much your investment will be worth after 2 years.

Year #	Principal (p)	Interest Rate (r)	Time (t)	l = prt	Year End Amount (A = I + p)
0.5yr	\$3000	0.075	0.5	\$112.50	\$3112.50
1 yr	\$3112.50	0.075	0.5	\$116.72	\$3229.22
1.5 yr	\$3229.22	0.075	0.5	\$121.10	\$3350.32
2 yr	\$3350.32	0.075	0.5	\$125.64	\$3475.96

5.) You invest \$1250 at an interest rate of 2.5% compounded quarterly. Calculate how much compound interest you will have earned on this investment after 1 year.
Problem #5

5.) You invest \$1250 at an interest rate of 2.5% compounded quarterly. Calculate how much compound interest you will have earned on this investment after 1 year.

Year#	Р	R	Т	l = prt	A = I + p
3 mos	\$1250	0.025	0.25		
6 mos					
9 mos					
12 mos					



Bryan puts \$800 into a bank account. It earns ¾ % interest semi-annually. How much money will he have after 1 year?



Bryan puts \$800 into a bank account. It earns ¾ % interest semi-annually. How much money will he have after 1 year?



- Students will:
- a) Apply the compound interest <u>formula</u> to calculate the amount of money in a savings account after a period of time
- b) Find the principal necessary for a savings account with compounded interest, given a specified money goal

Review from Tuesday

- Compound interest a way of calculating interest, in which you must calculate interest and a <u>new</u> principal after each period of time
- We STILL USE the interest formula
 I = p r t
- But there are many more STEPS
- This results in our principals and interest amounts growing... so our money grows more quickly!! ^(C)





Annually – once a year

Semi-annually – 2x a year (every 6 mos)

Quarterly – 4x a year (every 3 mos)

On your own... Please finish the compound interest worksheet and submit for a grade!!!



Month#	Ρ	r	t	l = prt	A = I + p
3			0.25		
6					
9					

Month#	Ρ	r	t	l = prt	A = I + p
3	\$100	0.022	0.25		
6					
9					

Month#	Ρ	r	t	l = prt	A = I + p
3	\$100	0.022	0.25	\$0.55	\$100.55
6	\$100.5 5	0.022	0.25	\$0.55	\$101.10
9	\$101.1 0	0.022	0.25	\$0.56	\$101.66

Look at your answer to #6 on the worksheet...

Simple Interest:

Compound Interest:

Look at your answer to #6 on the worksheet...

Simple Interest: $I = 500 \times 0.005 \times 4 = $10 \text{ A} = 500 + 10 = 510 Compound Interest:

Look at your answer to #6 on the worksheet...

Simple Interest: $I = 500 \times 0.005 \times 4 = $10 A = 500 + 10 = 510

Compound Interest: 1st yr: I = 500 x 0.005 x 1 = \$2.50 A = \$502.50

 2^{nd} yr: I = 502.50 x 0.005 x 1 = \$2.51 A = \$505.01

 3^{rd} yr: I = 505.01 x 0.005 x 1 = \$2.53 A = \$507.54

4th yr: I = 507.54 x 0.005 x 1 = \$2.54 A = \$510.08

Look at your answer to #6 on the worksheet...

Simple Interest: \$510 after 3 years

Compound Interest: \$510.08 after 3 years



Time

An easier way to do Compound Interest



- ♦ A = total money in account
- p = principal
- r = interest rate
- n = number of compoundings in a year
- t = time (years)

Let's work together on the <u>new</u> worksheet problems



1.) Shalika puts \$650 into a savings account that pays 1/5 % interest per year, compounded annually. What is the amount of money that she will have after 10 years?



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$$=$$
 \$650 r = 1/5 % t = 10 n = 1 (annual)

1.) Shalika puts \$650 into a savings account that pays 1/5 % interest per year, compounded annually. What is the amount of money that she will have after 10 years?



r =\$650 r = 1/5 % t = 10 n = 1 (annual) r = 0.2%

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 $A = P\left(1 + \frac{r}{n}\right)^{nt} = \frac{650}{r} = \frac{1}{5} \% \quad t = 10 \quad n = 1 \text{ (annual)}$ r = 0.2%r = 0.002 $A = 650 (1 + (0.002/1))^{(1 \times 10)}$

1.) Shalika puts \$650 into a savings account that pays 1/5 % interest per year, compounded annually. What is the amount of money that she will have after 10 years?



 $P = \$650 \quad r = 1/5 \% \quad t = 10 \quad n = 1 \text{ (annual)}$ r = 0.2%r = 0.002 $A = 650 (1 + (0.002/1))^{(1 \times 10)}$

A = 663.1176262 = **<u>\$663.12</u>**

2.) Darien invests \$10,000 in an account that pays 1.10% interest per year, compounded biannually. What is the amount of money that he will have after 3 years?



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$$P = $10,000$$
 $r = 1.10\%$ $t = 3$ $n = 2$
 $r = 0.011$

2.) Darien invests \$10,000 in an account that pays 1.10% interest per year, compounded biannually. What is the amount of money that he will have after 3 years?



$$P = $10,000$$
 $r = 1.10\%$ $t = 3$ $n = 2$
 $r = 0.011$

 $A = 10,000(1 + 0.011/2)^{(3 \times 2)}$

2.) Darien invests \$10,000 in an account that pays 1.10% interest per year, compounded biannually. What is the amount of money that he will have after 3 years?



$$P = $10,000$$
 $r = 1.10\%$ $t = 3$ $n = 2$
 $r = 0.011$

 $A = 10,000(1 + 0.011/2)^{(3 \times 2)}$ A = 10,334.57091 =**\$10,334.57**

6.) Tanesha has \$23,478.00 in a savings account paying 0.55% interest compounded quarterly. If she initially opened the account 15 years ago and didn't add nor take out any money from the account since she opened it, how much money did she initially deposit into the account (again, we're finding the starting



6.) Tanesha has \$23,478.00 in a savings account paying 0.55% interest compounded quarterly. If she initially opened the account 15 years ago and didn't add nor take out any money from the account since she opened it, how much money did she initially deposit into the account (again, we're finding the starting



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A =
$$$23,478.00$$
 r = 0.55% t = 15 n = 4
r = 0.0055

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23,478 = P(1.085937135)

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A =
$$$23,478.00$$
 r = 0.55% t = 15 n = 4
r = 0.0055

23,478 = P (1 + 0.0055/4)^(4 x 15) 23,478 = P (1.085937135) ÷ 1.085... ÷ 1.085...
Worksheet Problem #6

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Worksheet Problem #6

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A =
$$$23,478.00$$
 r = 0.55% t = 15 n = 4
r = 0.0055

 $23,478 = P (1 + 0.0055/4)^{(4 \times 15)}$ 23,478 = P (1,085937135) $\div 1.085... \div 1.085...$ $21,620.04 = P \qquad P = \$21,620.04$



 Franklyn puts \$2500 into a savings account paying 1.45% interest compounded semi-annually. How much money will he have 20 years later?



• Students will calculate the total money at the maturation date for a Certificate of Deposit.

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Place of Birth (POB)PHILIPPINES Item deposited: CASH BOND	Date of Birth (DDB); 19" MAY 1945 CLASSIFIED DOCUMENTS VALUABLES OTHERS (specify)
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Certificates of Deposit





What is a CD??

Certificate of deposit (CD) – a type of <u>investment</u> like a savings account, where the bank holds your money for a set period of time



What is a CD??

Certificate of deposit (CD) – a type of <u>investment</u> like a savings account, where the bank holds your money for a set period of time



- You cannot remove your money during this time period
- Interest rates are higher than for standard savings accounts
- The longer the term (time period) of the CD, the higher the interest rate
- The more money you put in a CD, the higher the interest rate

What is a CD?

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Other Names: Nationality: PH	ILIPPINE R\PH	s Lippines	MARIO	T NO 9300	AMBASSADOR
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CD maturation

- Maturation date the date you are able to take out your money + earned interest
- If you take our your money early, you forfeit interest + you pay a penalty fee!!!



Let's compare interest rates

What did we learn today?

Compound interest – interest that grows with the principal after each set increment of time

 Advantages of knowing compound interest:

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

1.) It is used more often than simple interest.

2.) It produces more *interest* (and therefore more money!! ☺) than simple interest.

Words to Remember:

- Certificate of Deposit (CD)
- Rate compounded daily
- APY (annual per year)
- Maturation date

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Deposited the sum of US\$22,500,000.00 (TWENTY TWO MILLION, FIVE HUNDRED THOUSAND USD)
A/C No:
on this day 4TH of FEBRUARY 2004
This Certificate is issued in accordance with the Hong Kong Banking Act of 1968 The Depositor/Beneficiary is expected to present this certificate in the event of transfer of funds to any nominated account. Please you are to tender this Certificate only on request.
Credit Officer Mindue Miles General Mapdage Carson



Mr. Dukat puts \$15,000 into a CD paying 0.7% compounded quarterly. How much total money will he have in his account 23 years from now?